

# A study of the oxidation kinetics of $\text{CuFeO}_2$ in the Cu-Fe-O system

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The oxidation kinetics of  $\text{CuFeO}_2$  in the Cu-Fe-O system have been studied between 500 and 900° C in an atmosphere containing 1 vol % oxygen in a nitrogen stream using thermogravimetric analysis (TGA). It was found that addition of  $\text{Fe}_2\text{O}_3$  to the  $\text{CuFeO}_2$  caused a decrease in the oxidation rate while addition of CuO caused an increase. On increasing the concentration of  $\text{Fe}_2\text{O}_3$  the activation energy was found to increase from  $\sim 18 \text{ kcal mol}^{-1}$  to  $\sim 45 \text{ kcal mol}^{-1}$  and the exponent 'n' in Avrami's equation  $f = 1 - \exp(-kt^n)$  was also observed to increase, from 1.3 to 2.3. On adding CuO to the  $\text{CuFeO}_2$  in the Cu-Fe-O system the activation energy decreased from  $\sim 18 \text{ kcal mol}^{-1}$  to  $\sim 8 \text{ kcal mol}^{-1}$ . The variation in both values indicates changes in the oxidation mechanisms. The microstructural changes associated with oxidation have been studied using optical microscopy. A model has been proposed to explain the results.

## 1. Introduction

Copper ferrite is a compound of two transition metal oxides. The valency states of the metallic ions depend on various factors such as the ratio of the metallic ion concentrations, the temperature and the surrounding atmosphere [1]. Therefore, several possible phases, e.g.  $\text{CuFe}_2\text{O}_4$ ,  $\text{CuFeO}_2$  and  $\text{CuFe}_5\text{O}_8$  exist in the Cu-Fe-O system [2-5]. In an earlier paper, the authors [1] studied the oxidation of  $\text{CuFeO}_2$  to  $\text{CuFe}_2\text{O}_4$  and simultaneous precipitation of CuO. The oxidation rate was reported to be maximum at a temperature of 700° C. Both, above and below this temperature, the oxidation rate decreased and depended entirely on the ionic mobility and partial pressure of the oxygen in the surrounding atmosphere.

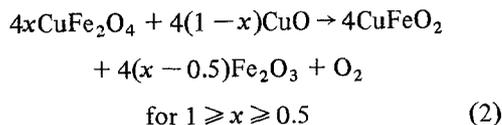
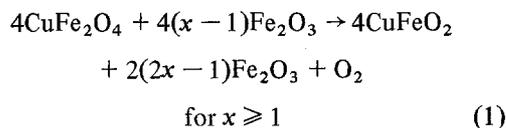
The present work deals with the oxidation of  $\text{CuFeO}_2$  to  $\text{CuFe}_2\text{O}_4$  when  $\text{Cu}_2\text{O}$  or  $\text{Fe}_2\text{O}_3$  is present as a second phase. The resulting microstructural changes have also been studied.

## 2. Experimental procedure

### 2.1. Material preparation

In order to prepare material with various compositions, reagent grades of copper oxide and ferric

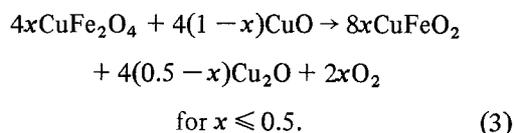
oxide in different molar ratios were mixed in a jar ball mill (shown in Table I). The resultant mixtures were pre-fired at 800° C for 10 h in air and ball milled again to obtain submicron size powders of homogenous composition. X-ray examination of pre-fired powders revealed the present of  $\text{CuFe}_2\text{O}_4$  and CuO or  $\text{Fe}_2\text{O}_3$  phases, depending on whether 'x' is less than or more than 1 respectively. To obtain a polycrystalline powder of  $\text{CuFeO}_2$ , the pre-fired powders were heated in an inert atmosphere at 900° C in a thermobalance [6]. The weight loss in each sample agreed well with the calculated weight loss for one or other of the following reduction reactions.



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TABLE I Chemical composition of the samples

Sample number	$x$ (mol)	Nominal composition of the oxidation	General formula
1	0.33	CuO:0.33Fe <sub>2</sub> O <sub>3</sub>	—
2	0.50	CuO:0.5 Fe <sub>2</sub> O <sub>3</sub>	—
3	1.00	CuO:1.0 Fe <sub>2</sub> O <sub>3</sub>	(CuO(Fe <sub>2</sub> O <sub>3</sub> ) <sub><math>x</math></sub> )
4	1.5	CuO:1.5 Fe <sub>2</sub> O <sub>3</sub>	—
5	2.0	CuO:2.0 Fe <sub>2</sub> O <sub>3</sub>	—
6	2.5	CuO:2.5 Fe <sub>2</sub> O <sub>3</sub>	—



Thus CuFeO<sub>2</sub> with Cu<sub>2</sub>O or Fe<sub>2</sub>O<sub>3</sub> was obtained as a second phase. These were further checked by X-ray analysis of the quenched samples held at 900° C in a nitrogen atmosphere.

## 2.2. Thermogravimetric analysis

In order to study the kinetics of the oxidation of CuFeO<sub>2</sub> in the presence of Cu<sub>2</sub>O or Fe<sub>2</sub>O<sub>3</sub>, the samples were cooled from 900° C down to various temperatures in a nitrogen atmosphere. Such a cooling under nitrogen caused no increase in the weight of the sample, indicating that the samples were not oxidized on cooling to the temperature of interest. 1 vol% oxygen was added to the nitrogen stream and the gain in weight of the sample was monitored isothermally until the weight remained constant. The oxidized samples were analysed by X-ray analysis (Table II) and the presence of CuFe<sub>2</sub>O<sub>4</sub>, CuFeO<sub>2</sub>, CuO or Fe<sub>2</sub>O<sub>3</sub> was detected.

## 2.3. Metallography

The results of thermogravimetric and X-ray analysis were further confirmed by using optical microscopy. For this purpose, discs of the prefired and milled powders were pressed at a pressure of 1.2 tonne cm<sup>-2</sup>. The discs were sintered at 900° C

in a nitrogen atmosphere to obtain a CuFeO<sub>2</sub> phase and then quenched to examine the phases present. The surface of the discs was ground about 0.5 mm and polished well by the method given elsewhere [1]. The polished samples were etched in a solution of 50 vol% HCl + 0.5 mol% FeCl<sub>3</sub>. To study the mechanism of oxidation of CuFeO<sub>2</sub> to CuFe<sub>2</sub>O<sub>4</sub> and simultaneous dissolution of Fe<sub>2</sub>O<sub>3</sub>, the samples were heated in an oxygen atmosphere at 900° C for 1 min to 24 h and then quenched. Quenched samples were lapped, polished and thermally etched.

## 3. Experimental results

The isothermal weight changes in the reduced samples in an atmosphere containing nitrogen with 1 vol% oxygen are shown in Fig. 1 a to d. These curves are plotted for the mass of CuFeO<sub>2</sub> oxidized ( $\Delta W$ ) versus time ( $t$ ) between the temperatures 500 and 700° C. All the curves show an incubation period which varies with temperature and composition.

The curves in Fig. 1a shows that the oxidation followed a rectilinear law ( $\Delta W \propto t$ ). The oxidation of CuFeO<sub>2</sub> is of a nucleation and growth type process as described earlier [1]. In fact, this composition has two phases: CuFeO<sub>2</sub> and Cu<sub>2</sub>O, where oxidation of Cu<sub>2</sub>O to CuO in 1 vol% oxygen obeys the rectilinear oxidation law [7]. Oxidation of both the phases takes place simultaneously and this is a case of mixed oxidation.

Curves for  $\Delta W$  against time were plotted for

TABLE II X-ray analysis of phases present

$x$ (mol)	Prefired samples composition	Sample composition in a nitrogen atmosphere at 900° C	Sample composition in an oxygen atmosphere at 500 to 700° C
0.33	CuFe <sub>2</sub> O <sub>4</sub> + CuO	CuFeO <sub>2</sub> + Cu <sub>2</sub> O	—
0.5	—	CuFeO <sub>2</sub>	CuFe <sub>2</sub> O <sub>4</sub> + CuO
1.0	CuFe <sub>2</sub> O <sub>4</sub>	CuFeO <sub>2</sub> + Fe <sub>2</sub> O <sub>3</sub>	—
1.5	CuFe <sub>2</sub> O <sub>4</sub> + Fe <sub>2</sub> O <sub>3</sub>	CuFe <sub>2</sub> O <sub>4</sub> + Fe <sub>2</sub> O <sub>3</sub>	—
2.0	—	—	—
2.5	CuFe <sub>2</sub> O <sub>4</sub> + Fe <sub>2</sub> O <sub>4</sub>	—	—

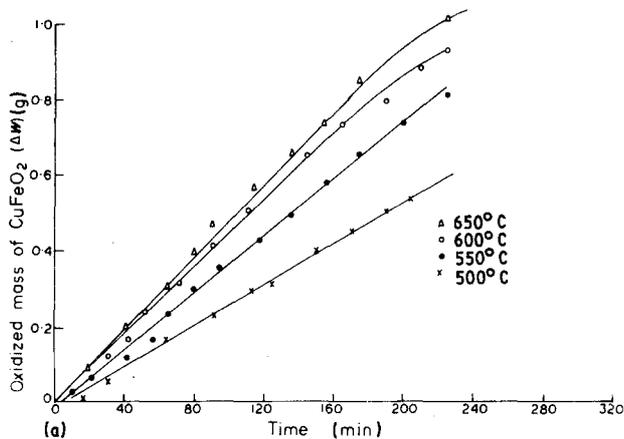
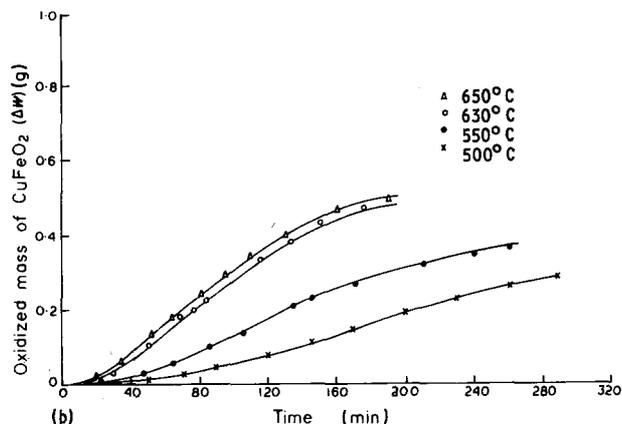


Figure 1 Oxidation of  $\text{CuFeO}_2$  as a function of time, temperature and composition  $[\text{CuO}(\text{Fe}_2\text{O}_3)_x]$  (a)  $x = 0.5$  (b)  $x = 1.5$  (c)  $x = 2.0$  and (d)  $x = 2.5$ .



all compositions, which were oxidized at  $600^\circ\text{C}$ . These are shown in Fig. 2. These curves show that for an equal time, a different amount of  $\text{CuFeO}_2$  oxidized on decreasing the value of  $x$ . Hence, it may be concluded that the oxidation rate decreased on increasing the concentration of  $\text{Fe}_2\text{O}_3$  in the composition.

Similar to the previous work [1], these oxidation data were also found to fit best to Avrami's equation [8]

$$f = 1 - \exp(-kt^n) \quad (4)$$

where  $f$  is  $\Delta W/W$ , the mass fraction oxidized,  $t$  is time,  $k$  is oxidation rate constant and  $n$  is the exponent.

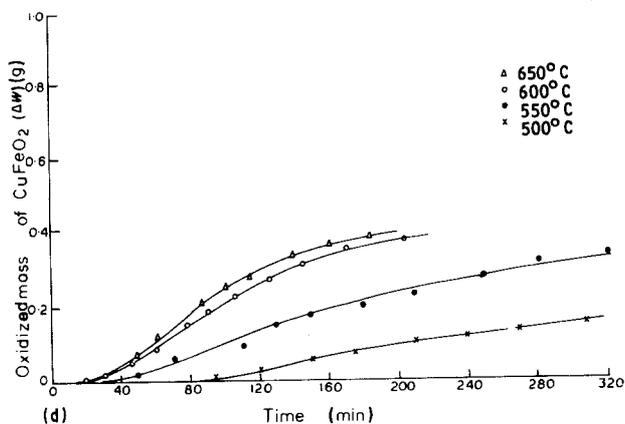
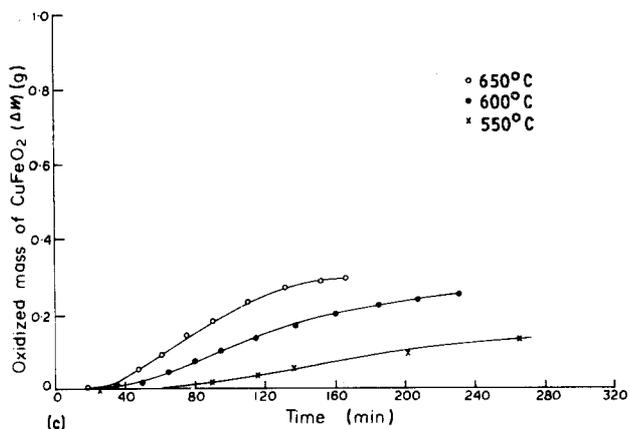
Fig. 3 shows  $\ln \ln(1/(1-f))$  against  $\ln(t)$  plots of Equation 4 for composition 4 of Table I. Other compositions in Table I gave similar types of plots. The slope and intercept of these plots give the value of the exponent  $n$  and the rate constant  $k$  respectively. Exponent  $n$  was found to vary from 1.3 to 2.3 as shown in Fig. 4 and the rate constant,  $k$ , from  $3 \times 10^{-5}$  to  $1 \times 10^{-10} \text{sec}^{-1}$

(Table III) as  $x$  varied from 0.3 to 2.5. The variation in the value of exponent  $n$  denotes that the oxidation of  $\text{CuFeO}_2$  to  $\text{CuFe}_2\text{O}_4$  in the presence of  $\text{Fe}_2\text{O}_3$  changes from a one dimensional oxidation process to a two dimensional oxidation process [9]. These results indicate that the variation in the oxidation rate constant,  $k$ , for the oxidation of  $\text{CuFeO}_2$  to  $\text{CuFe}_2\text{O}_4$  apart from being dependent on the temperature and surrounding atmosphere also depends upon the Fe/Cu ratio.

The activation energy for the oxidation of  $\text{CuFeO}_2$  to  $\text{CuFe}_2\text{O}_4$  in the presence of  $\text{Cu}_2\text{O}$  and  $\text{Fe}_2\text{O}_3$  in the Cu-Fe-O system has been calculated from the Arrhenius plots of the rate constants. The value of the activation energy has been found to be nearly equal for the samples for which  $x$  varies from 0.5 to 1.0.

The microstructure of the samples in Table I which were sintered at  $900^\circ\text{C}$  for 36 h in a nitrogen atmosphere are shown in Fig. 5 a to f. Fig. 5b shows a single phase of  $\text{CuFeO}_2$  (which is a stable phase below  $1005^\circ\text{C}$  [10]) as detected by X-ray diffraction (XRD) analysis. XRD results of the

Figure 1 Continued.



samples also agreed well with the microstructures which are shown in Fig. 5 c to f. These microstructures show the presence of two phases. The concentration of the white phase was seen to vary as  $x$  varied from 1 to 2.5. Thus, from the microstructures of Figs. 5 c to f it can be concluded

that the grey and white phases are CuFeO<sub>2</sub> and Fe<sub>2</sub>O<sub>3</sub> respectively.

The black areas in the micrographs of Figs. 5 c to f are the pores, most of which lie near Fe<sub>2</sub>O<sub>3</sub>. The concentration of pores seems to increase as the concentration of Fe<sub>2</sub>O<sub>3</sub> increases. This may be

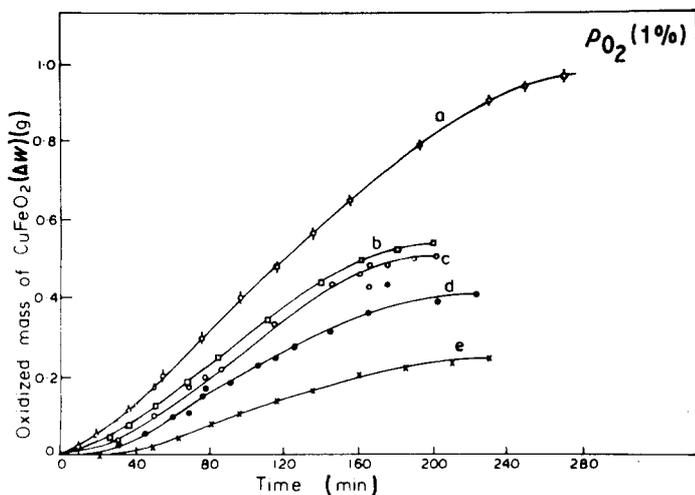


Figure 2 Oxidation of CuFeO<sub>2</sub> as a function of time and composition [CuO(Fe<sub>2</sub>O<sub>3</sub>)<sub>x</sub>] at 600°C (a)  $x = 0.5$  (b)  $x = 1.0$  (c)  $x = 1.5$  (d)  $x = 2.0$  and (e)  $x = 2.5$ .

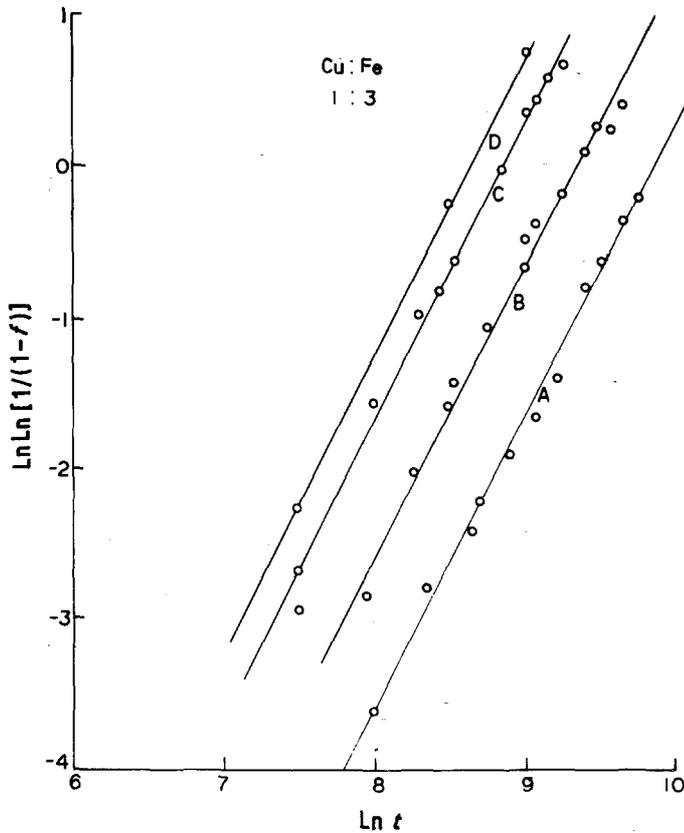


Figure 3 Plots of  $\ln \ln [1/(1-f)]$  against  $(t)$  for  $x = 1.5$ .

due to a lower sintering rate of the sample containing  $\text{Fe}_2\text{O}_3$  in excess of stoichiometry.

Fig. 6a shows the microstructure of the oxidized surface of the sample quenched from  $900^\circ\text{C}$  in air whose microstructure is shown in Fig. 5b. On the surface of the quenched sample some grey and white stripes are seen inside the grains. They are due to the oxidation of the surface during quench-

ing. These stripes inside the grains represent two different types of phase, i.e.  $\text{CuFe}_2\text{O}_4$  and  $\text{CuO}$ .

Fig. 6b shows the microstructure of the above sample after prolonged heating in the oxygen atmosphere. This microstructure is different from the microstructure presented in Fig. 6a.  $\text{CuO}$  is present as globules at the grain boundaries of  $\text{CuFe}_2\text{O}_4$  (in contrast with the lamellar pre-

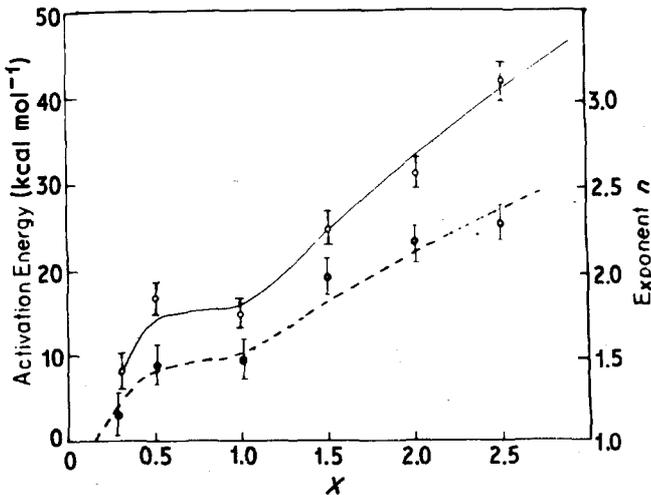


Figure 4 Plots of exponent  $n$  and activation energy against  $x$ .

TABLE III Rate constant at various temperatures

Composition	$k$ (sec <sup>-1</sup> )				
	500° C	550° C	600° C	650° C	700° C
CuFeO <sub>2</sub> + Cu <sub>2</sub> O	$1.3 \times 10^{-5}$	$1.67 \times 10^{-5}$	$2.14 \times 10^{-5}$	$3.36 \times 10^{-5}$	—
CuFeO <sub>2</sub>	$5.57 \times 10^{-7}$	—	$2.0 \times 10^{-6}$	—	$7.5 \times 10^{-6}$
2CuFeO <sub>2</sub> + Fe <sub>2</sub> O <sub>3</sub>	$6.48 \times 10^{-7}$	—	—	$3.23 \times 10^{-7}$	$4.57 \times 10^{-6}$
CuFeO <sub>2</sub> + Fe <sub>2</sub> O <sub>3</sub>	$3.39 \times 10^{-9}$	$9.71 \times 10^{-9}$	$2.5 \times 10^{-8}$	$3.74 \times 10^{-8}$	—
2CuFeO <sub>2</sub> + 3Fe <sub>2</sub> O <sub>3</sub>	$3.56 \times 10^{-10}$	$1.189 \times 10^{-9}$	$4.36 \times 10^{-9}$	$6.84 \times 10^{-9}$	—
CuFeO <sub>2</sub> + 2Fe <sub>2</sub> O <sub>3</sub>	$1.69 \times 10^{-10}$	$9.736 \times 10^{-10}$	$3.398 \times 10^{-9}$	$1.186 \times 10^{-9}$	—

precipitation of Fig. 6a). When  $x \geq 1$ , CuO is not seen in the microstructures as shown in Fig. 7 b to e. Fig. 7b shows a single CuFe<sub>2</sub>O<sub>4</sub> phase, which is stable up to 1050° C in an oxygen atmosphere.

Fig. 7 c to e shows two phases (one is grey and other is white). These are CuFe<sub>2</sub>O<sub>4</sub> and Fe<sub>2</sub>O<sub>3</sub> as per X-ray analysis. The concentration of white phase increases with  $x$  which confirms that the

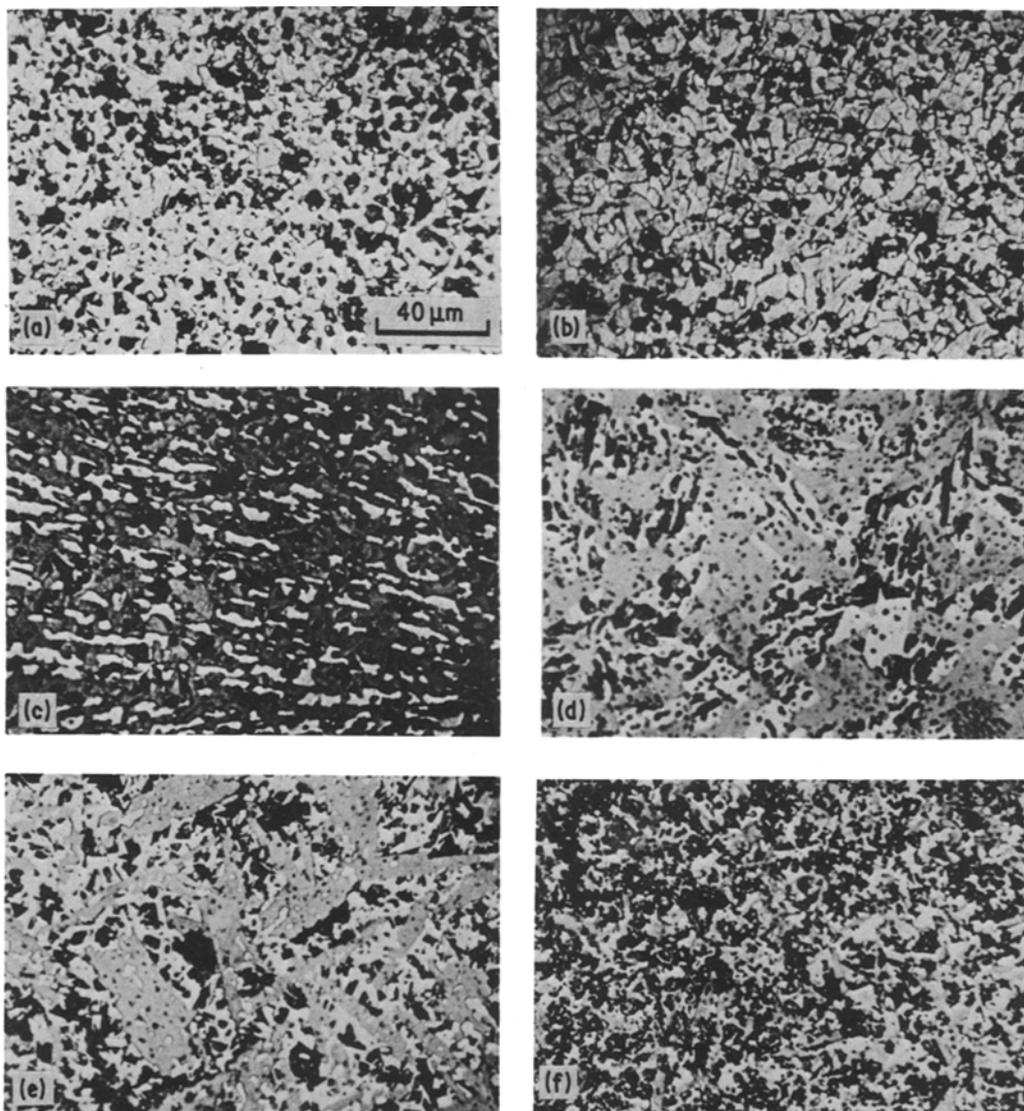


Figure 5 Microstructures of different compositions [CuO(Fe<sub>2</sub>O<sub>3</sub>)<sub>x</sub>] in the Cu–Fe–O system sintered at 900° C in a nitrogen atmosphere and quenched (a)  $x = 0.33$  (b)  $x = 0.5$  (c)  $x = 1.0$  (d)  $x = 1.5$  (e)  $x = 2.0$  and (f)  $x = 2.5$ .

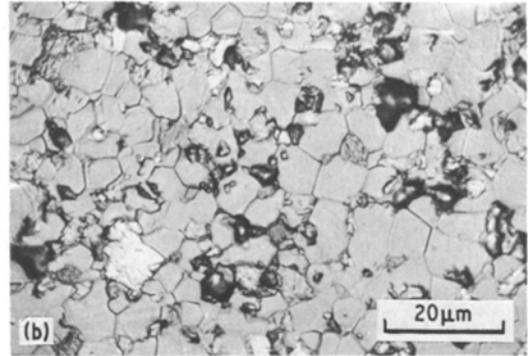
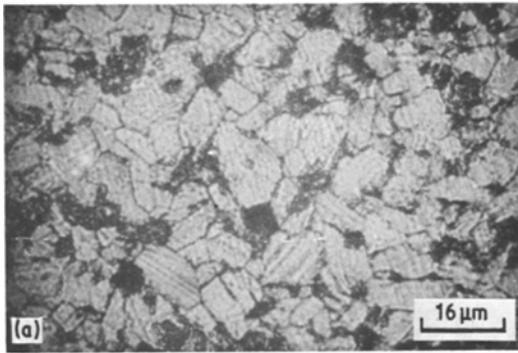


Figure 6 (a) Microstructure of the sample with composition 6 (Table I) after complete oxidation.

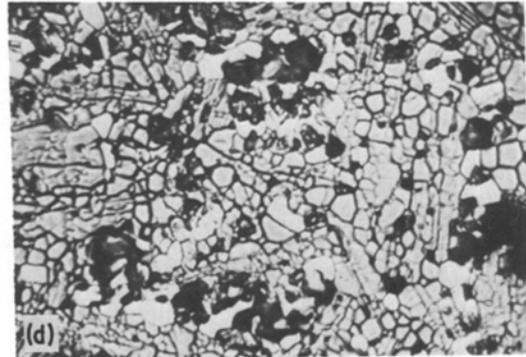
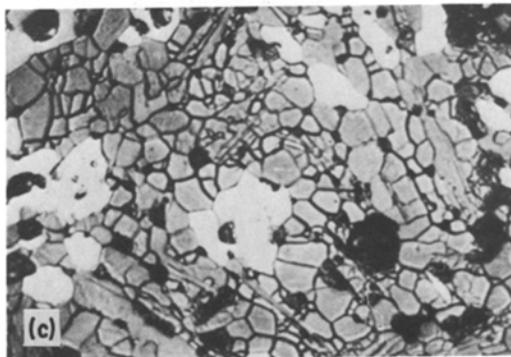
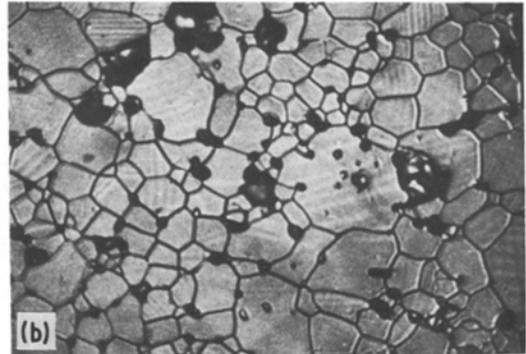
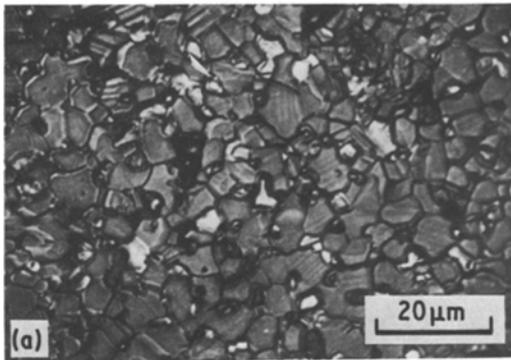


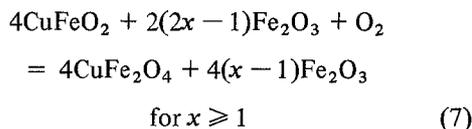
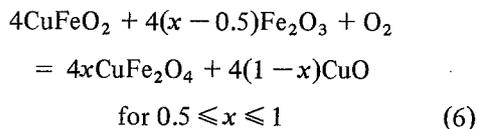
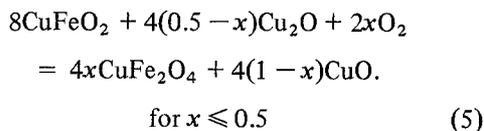
Figure 7 Microstructures of the oxidized samples of different compositions shown in Fig. 5 b to f (a)  $x = 0.5$  (b)  $x = 1.0$  (c)  $x = 1.5$  (d)  $x = 2.0$  and (e)  $x = 2.5$ .

grey phase is  $\text{CuFe}_2\text{O}_4$  and the white phase is  $\text{Fe}_2\text{O}_3$ . In the Cu-rich sample shown in Fig. 7a,  $\text{CuO}$  precipitated along  $\text{CuFe}_2\text{O}_4$  grains giving a microstructure similar to Fig. 6b. On comparing the microstructures of Fig. 7 b to e with Fig. 5 c to f, i.e. the volume fraction of  $\text{CuFe}_2\text{O}_4$  seems to be more than that of  $\text{CuFeO}_2$ . Thus in the presence of oxygen in the atmosphere, interdiffusion between  $\text{CuFeO}_2$  and  $\text{Fe}_2\text{O}_3$  took place and excess  $\text{CuO}$  or  $\text{Fe}_2\text{O}_3$  precipitated.

#### 4. Discussion

The results presented in Section 3 show that the samples of the Cu-Fe-O system in the reduced state have two phases i.e.  $\text{CuFeO}_2$  and  $\text{Cu}_2\text{O}$  or  $\text{Fe}_2\text{O}_3$  depending upon the composition. The oxidation of the sample ( $\text{CuFeO}_2$ ) takes place when the equilibrium oxygen partial pressure ( $p_{\text{O}_2}^{\text{eq}}$ ) of the composition is less than oxygen partial pressure ( $p_{\text{O}_2}$ ) in the surrounding atmosphere, i.e.  $p_{\text{O}_2} > p_{\text{O}_2}^{\text{eq}}$ . Under the above conditions the sample adsorbs oxygen. The adsorbed oxygen acquires an electron from neighbouring Cu ions. Thus Cu ions become more positively charged and a metastable phase of " $\text{Cu}_2\text{Fe}_2\text{O}_5$ " is formed. From this metastable phase the stable phases  $\text{CuFe}_2\text{O}_4$  and  $\text{CuO}$  nucleate and grow in composition 3 of Table I. For a composition  $x \geq 1$ ,  $\text{Fe}_2\text{O}_3$  is present with  $\text{CuFeO}_2$  and this  $\text{Fe}_2\text{O}_3$  reacts with the oxidized metastable phase to give  $\text{CuFe}_2\text{O}_4$ , which is stable as shown in Fig. 8.

The oxidation of the samples at the surface may be explained by one or the other of the following equations.



Equations 5, 6 and 7 show that for all compositions with  $x < 1$ ,  $\text{CuO}$  precipitates out and for  $x \geq 1$ , a part of the second phase  $\text{Fe}_2\text{O}_3$  which is already present dissolves. For further oxidation

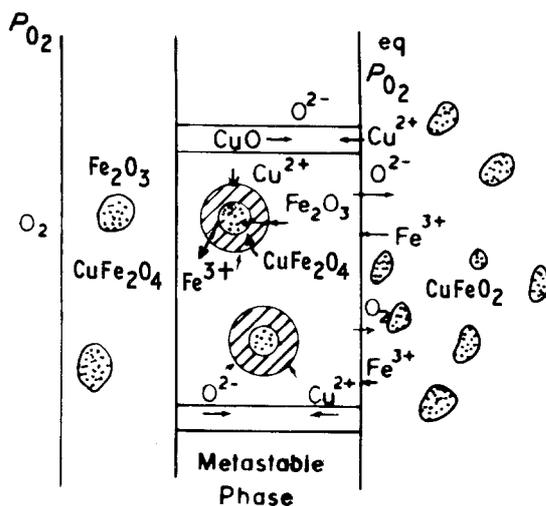


Figure 8 Schematic representation of the oxidation of  $\text{CuFeO}_2$  with non-stoichiometric composition.

of the sample anions or cations should diffuse through the  $\text{CuO}$ ,  $\text{CuFe}_2\text{O}_4$  or  $\text{Fe}_2\text{O}_3$  phases.

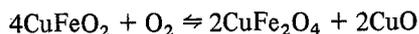
In the present work the activation energy for the oxidation of  $\text{CuFeO}_2$  is the same for compositions 2 and 3 in Table I. The same values of activation energy for two different compositions indicates that in this composition range the mechanism of diffusion of ions during oxidation is the same. The results also indicate that in compositions 2 and 3  $\text{CuO}$  precipitates in the oxidized layer. This together with the observation that the activation energy increases when  $\text{CuO}$  disappears as a second phase for  $x > 1$ , strongly suggests that diffusion of ions in the oxidized layer is predominantly through  $\text{CuO}$  when it is present. It is also well known that the activation energy for the diffusion of Cu ions through  $\text{CuO}$  is  $18 \text{ kcal mol}^{-1}$  [11] whereas that for the diffusion of metal ions through a spinel lattice, range from 50 to  $150 \text{ kcal mol}^{-1}$  [11].

The activation energy of oxidation increases significantly on increasing  $x$  above 1. The exponent  $n$  also increases in this region indicating a possible change in mechanism of oxidation. Beyond the composition with  $x$  equal to 1, no  $\text{CuO}$  phase is stable in the oxidized region and the increase in  $n$  from 1.3 to 2.3 indicates that the oxidation process becomes a two dimensional one. This is expected since in this composition range, as discussed earlier, oxidation proceeds by formation of an oxygen rich metastable phase, which converts to  $\text{CuFe}_2\text{O}_4$  by interdiffusion of ions as shown in Fig. 8.

The interdiffusion process of  $\text{Cu}^{2+}$  and  $\text{Fe}^{3+}$  ions between  $\text{Fe}_2\text{O}_3$  and metastable ( $\text{Cu}_2\text{Fe}_2\text{O}_5$ ) phases seems to be similar to the interdiffusion of metal ions between metallic oxide systems like  $\text{MgO}-\text{Al}_2\text{O}_3$ ,  $\text{MgO}-\text{Fe}_2\text{O}_3$  etc. [11]. The activation energy for the diffusion process of oxygen or metal ions in  $\text{Fe}_2\text{O}_3$  and spinel ferrites varies from 50 to  $150\text{ kcal mol}^{-1}$  [11]. In the  $\text{Cu}-\text{Fe}-\text{O}$  system not only the interdiffusion of  $\text{Cu}/\text{Fe}$  ions between the  $\text{Fe}_2\text{O}_3$  and the metastable phase is taking place but also the nucleation of  $\text{CuO}$ , which is also a prominent factor.

The activation energy for the diffusion of the  $\text{Cu}-\text{Fe}-\text{O}$  system is found to decrease on decreasing  $x$  below 0.5. Samples with these compositions have two phases i.e.  $\text{CuFeO}_2$  and  $\text{Cu}_2\text{O}$  in the reduced state. For these, adsorption of oxygen ions and the recombination of the diffusing ions become the rate controlling factors. For adsorption and recombination the activation energy is very low [12]. Therefore, it can be concluded that on increasing the concentration of  $\text{Cu}_2\text{O}$  the adsorption and recombination processes start to dominate, resulting in a lower activation energy.

A model proposed for explaining the oxidation of powdered material of stoichiometric composition agrees quite well with the microstructure shown in Fig. 6a. The grey and white lines inside the grains represent two products of the oxidation of  $\text{CuFeO}_2$ . These are  $\text{CuFe}_2\text{O}_4$  and  $\text{CuO}$ , according to the reaction



because in an oxygen atmosphere only  $\text{CuFe}_2\text{O}_4$ ,  $\text{CuO}$  and  $\text{Fe}_2\text{O}_3$  are stable. Prolonged heating of  $\text{CuFeO}_2$  in an oxygen atmosphere causes  $\text{CuO}$  to spheroidize and such spheroids of  $\text{CuO}$  are found at the grain boundaries of  $\text{CuFe}_2\text{O}_4$ . In the non-stoichiometric compositions, interdiffusion

between  $\text{CuFeO}_2$  and  $\text{Fe}_2\text{O}_3$  starts to form  $\text{CuFe}_2\text{O}_4$  at the interfaces. This reaction continues until the  $\text{CuFeO}_2$  phase completely disappears. This is a slow process, therefore, on prolonged oxidation grains of  $\text{CuFe}_2\text{O}_4$  also begin to grow. Excess  $\text{Fe}_2\text{O}_3$ , greater than the stoichiometric composition of  $\text{CuFe}_2\text{O}_4$ , remains unreacted at some places.

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